

## Objectives :

- to understand the phase shift between the voltage and current for an inductor,
- to learn inductive reactance for an inductor and impedance of an AC circuit.
- to determine the inductance value  $L$  of an
- to learn how to use cathode-ray oscilloscope.

## Equipment Used :

- coil with  $N = 1600$  turns.
- function generator.
- variable resistance box.
- CRO with cro probe and few wires.
- two multimeters.

I) RL circuit

- The emf of the source is given by

$\mathcal{E}(t) = \mathcal{E}_m \sin \omega t = V_L$ , where  $V_L$  is the voltage across the inductor.

$$- \frac{di}{dt} = \frac{V_L}{L} = \frac{V_{Lm}}{L} \sin \omega t$$

$\Rightarrow i_L = i_{Lm} \sin(\omega t - 90^\circ)$  where  $X_L$  is the inductive reactance of the inductor and

$$i_L = \frac{V_L}{X_L}$$

- In RL circuit,  $i_L$  lags  $V_L$  by  $\pi/2$  where  $i_R$  and  $V_R$  are in phase.

$$- \mathcal{E}_m = V_{Rm} + V_{Lm} \Rightarrow \mathcal{E} = V_R + V_L$$

By Ohm's Law,  $i^2 Z^2 = i^2 R^2 + i^2 X_L^2$ .

$\Rightarrow Z^2 = R^2 + X_L^2$ , where  $Z$  is the impedance of the circuit.

⇒ By considering the internal resistances

of the coil's wires,  $z^2 = (R+r)^2 + X_L^2$ .

- The plot of  $z^2$  versus  $(R+r)^2$  is a straight line with y-intercept =  $X_L^2 \Rightarrow L = \frac{X_L}{2\pi}$

## II) Cathode-ray Oscilloscope (CRO).

- A device used to visualize AC signals.

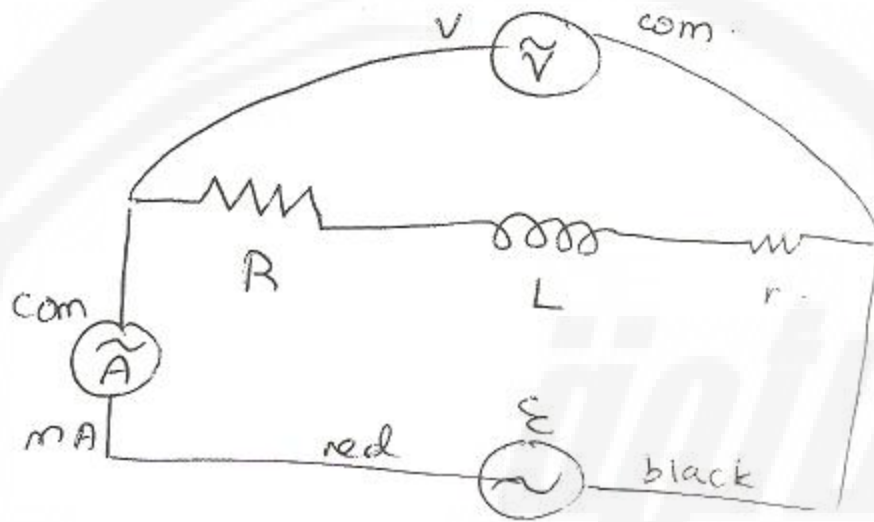
All controls are self explained and marked on the front panel.

## III) Root - mean - square (rms).

$$- \Sigma_{rms} = \sqrt{\frac{1}{T} \int_0^T \Sigma_m^2 \sin^2(\omega t) dt}$$

$$\Rightarrow \Sigma_{rms} = \frac{\Sigma_m}{\sqrt{2}} = \frac{\Sigma_{p-p}}{2\sqrt{2}}$$

where  $\Sigma_{p-p}$  is the peak to peak voltage,



function generator

$$f = 250 \text{ Hz}$$

Fig (I) = connection diagram to measure  $V_T$  and  $I_T$ .

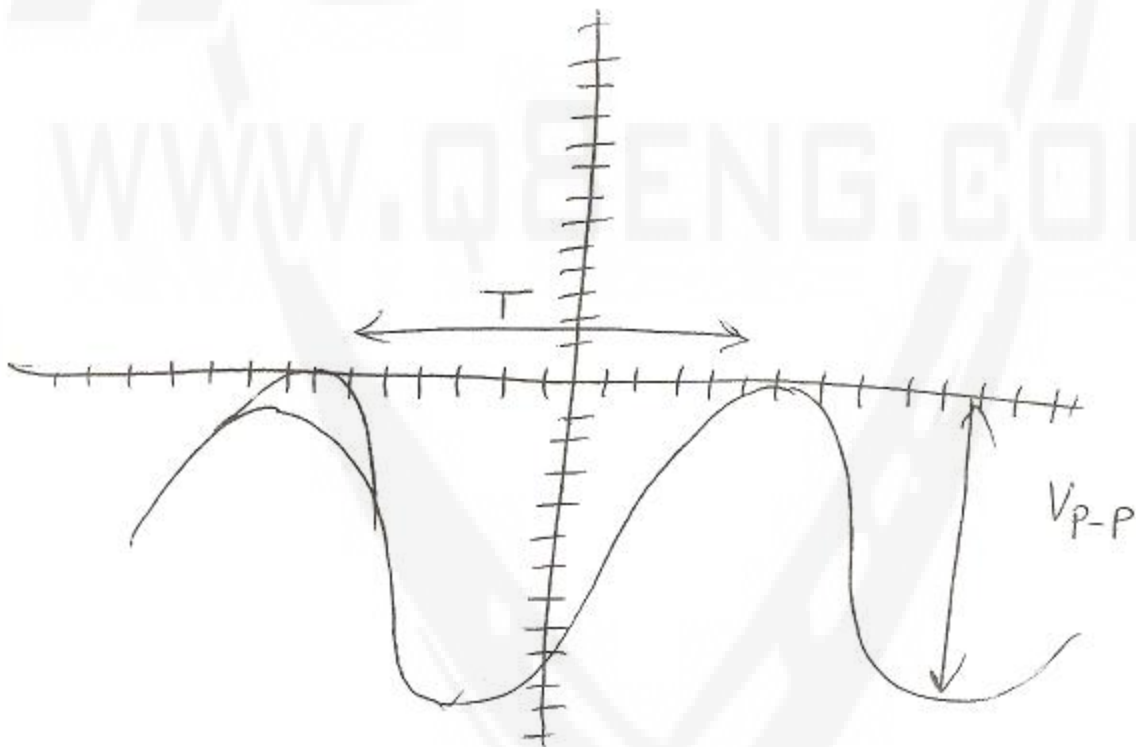


Fig (II) = AC signal on a CRO screen.

## \* Error sources :

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- \* Loose connections.
- \* Inaccuracy in taking Results.
- \* System errors.

## Procedure :

Part I , V, I measurements using multimeter

- 1- Set M.M to Ohm. connect the circuit as shown in Fig 1. after measuring the internal resistance  $r$  of the coil.
- 2 - Set the function generator to sine wave, frequency = 250 Hz. and maximum amplitude.
- 3 - Change the resistance  $R$  as in table and measure  $V_T$  and  $I_T$  through the circuit.
- 4 - Calculate  $(R+r)^2$ ,  $Z$ , and  $Z^2$  for each  $R$ .
- 5 - Plot  $Z^2$  versus  $(R+r)^2$  and use it to determine  $X$  then calculate  $\dots$

\* Result comparison with  
accepted values

-  $X_L^2$  (from graph) =  $6 \times 10^3$

$\Rightarrow L$  (from the graph) =  $0.0493 \text{ H}$

$L$  (Theoretical) =  $50 \text{ mH} = 0.05 \text{ H}$

Data tables :

$R (\Omega)$	$(R+r)^2 (\Omega^2)$	$I_Z (A)$	$V_Z (V)$	$Z = \frac{V_Z}{I}$ ( $\Omega$ )	$Z^2 (\Omega^2)$
50	$7.02 \times 10^3$	$47.8 \times 10^{-3}$	5.44	113.8	$12.95 \times 10^3$
80	$12.95 \times 10^3$	$40.7 \times 10^{-3}$	5.65	138.8	$19.27 \times 10^3$
110	$20.68 \times 10^3$	$35.4 \times 10^{-3}$	5.87	165.8	$27.49 \times 10^3$
140	$30.21 \times 10^3$	$31.3 \times 10^{-3}$	6.05	193.3	$37.36 \times 10^3$
170	$41.53 \times 10^3$	$28.0 \times 10^{-3}$	6.21	221.8	$49.19 \times 10^3$

## \* possible Methods to avoid mistakes

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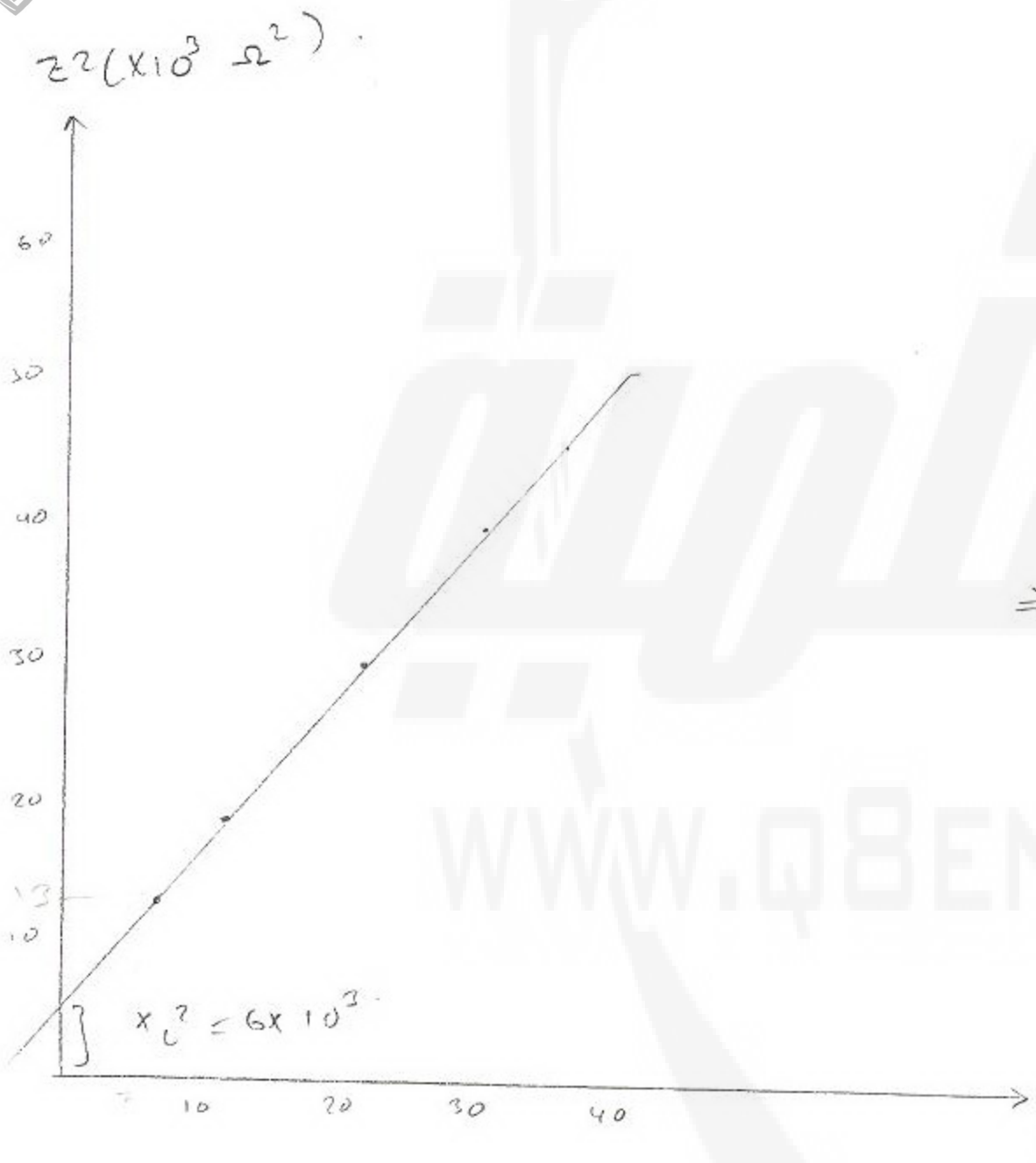
- taking reading accurately.
- connecting the wires carefully.
- doing the calculations properly.
- test devices before using them.

## \* General conclusion

- Voltage of the inductor leads the current by  $\pi/2$ .
- Inductors can be used as a storage element for energy.
- Internal resistance of the coil in RL circuits should be considered to get accurate values.

## \* Reference :

- physics university book



$$\Rightarrow L = \sqrt{\frac{X_c^2}{4\pi^2 f^2}} = 0.0493 \text{ H.}$$